



30°-60°-90° TRIANGLE

PROBLEM 1

PROBLEM 2

PROBLEM 3

45°-45°-90° TRIANGLE

PROBLEM 4

PROBLEM 5

PROBLEM 6

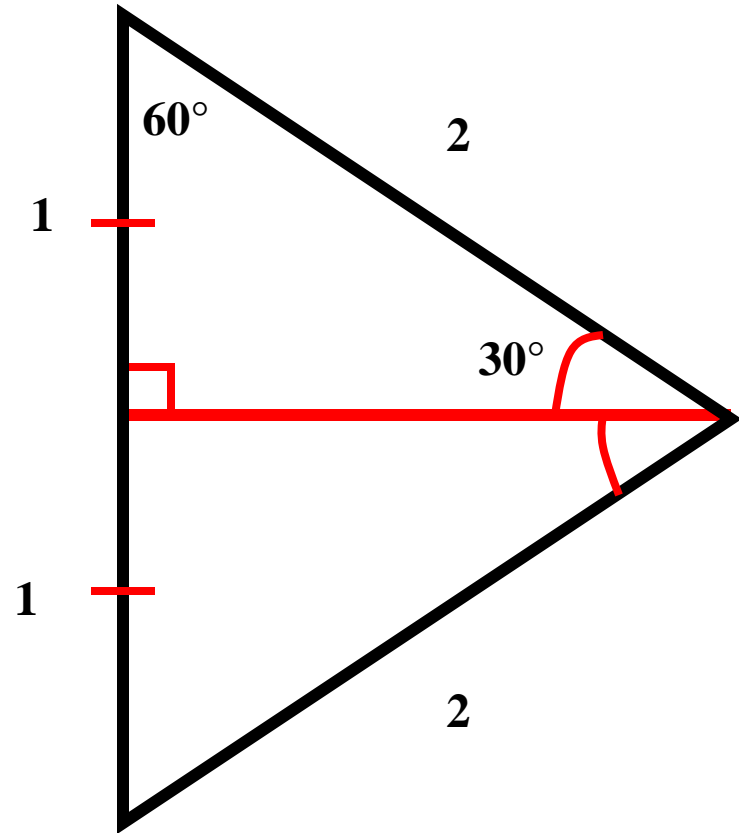
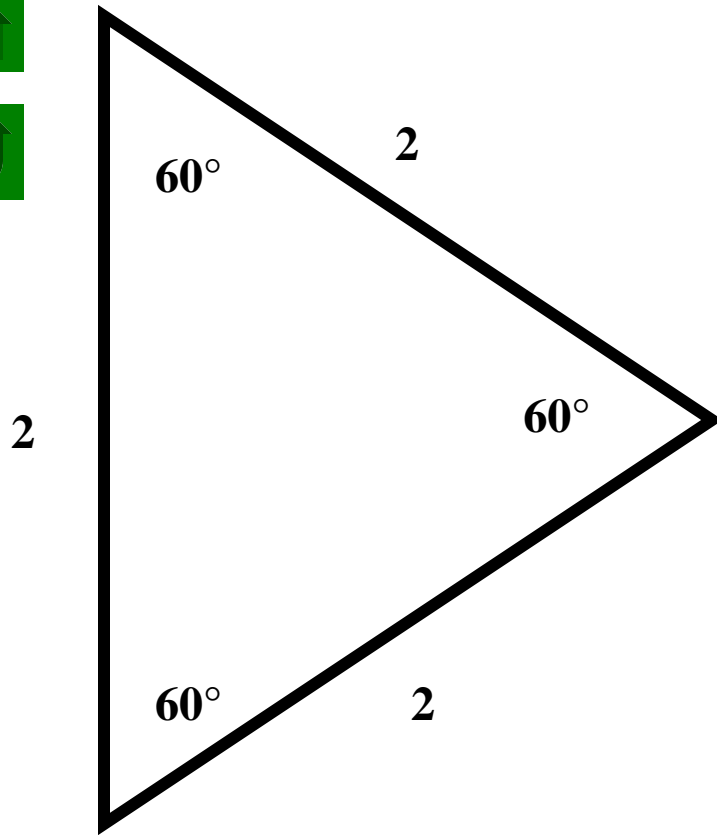
END SHOW



Standard 20:

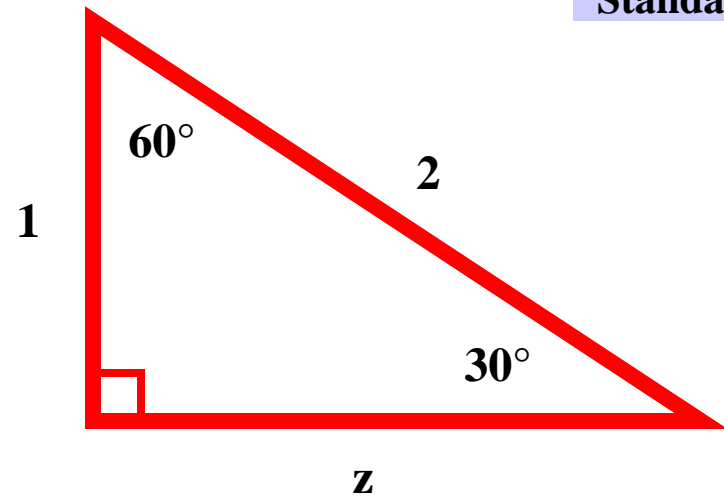
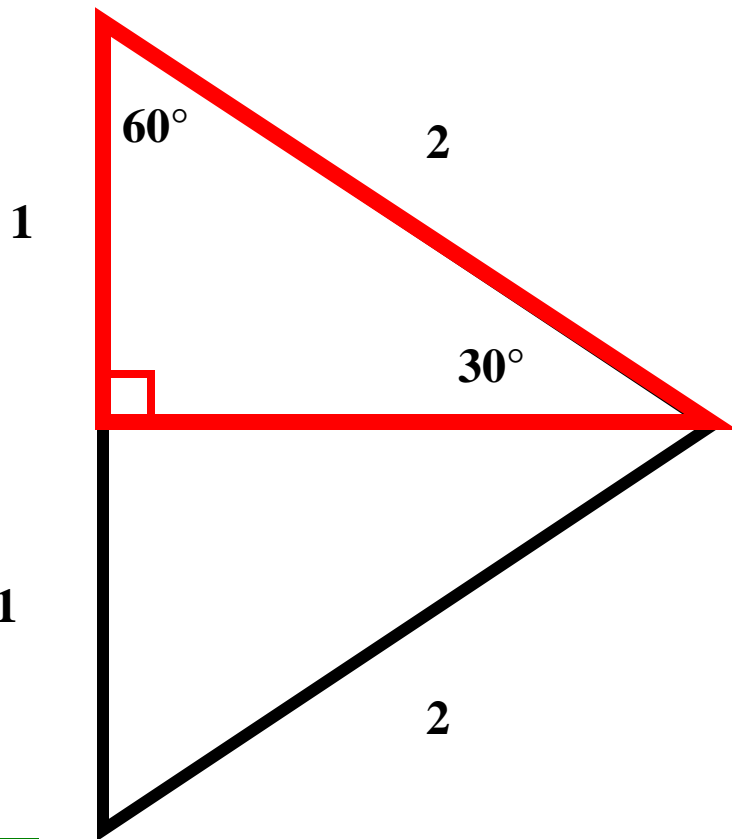
Students know and are able to use angle and side relationships in problems with special right triangles, given an angle and a length of a side.

Los estudiantes saben y son capaces de usar relaciones de lado y ángulo en problemas con triángulos especiales, dado un ángulo y la longitud de su lado.



1. An equilateral triangle is also equiangular, all angles are the same.
2. Let's draw an *Altitude* from one of the vertices. Which is also a *Median* and *Angle bisector*.
3. The bisected side is divided into two equal segments and the bisected angle has now two 30° equal angles.

How is the right angle that was formed? Click to find out



4. The triangle is divided into 2 right angles with acute angles of 30° and 60°



5. Let's draw the top triangle and label the unknown side as z .

6. Let's apply the Pythagorean Theorem to find the unknown side.

$$2^2 = z^2 + 1^2$$

$$4 = z^2 + \cancel{1}$$

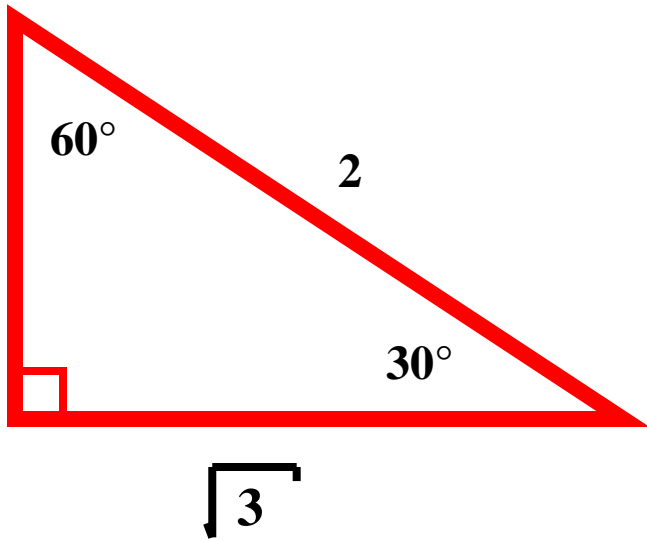
$$3 = z^2$$

$$z = \sqrt{3}$$

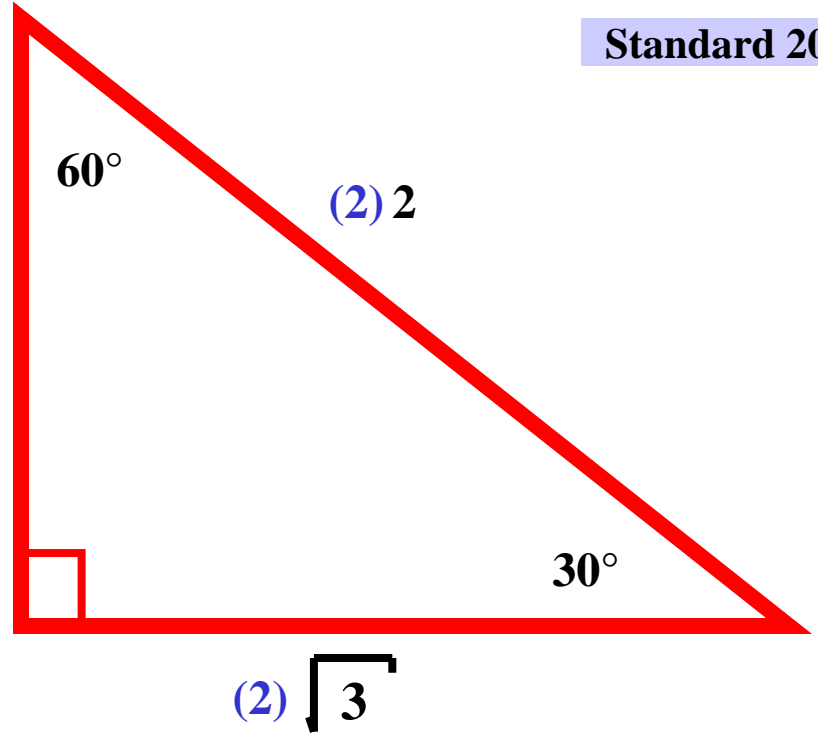
Can we generalize this result for all 30° - 60° - 90° right triangles? Click to find out... 4



1

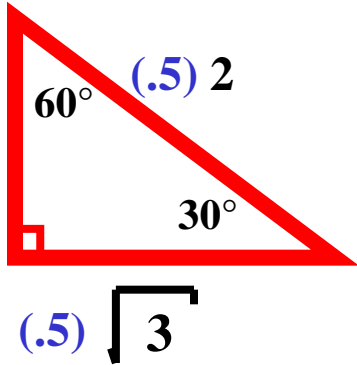


(2) 1



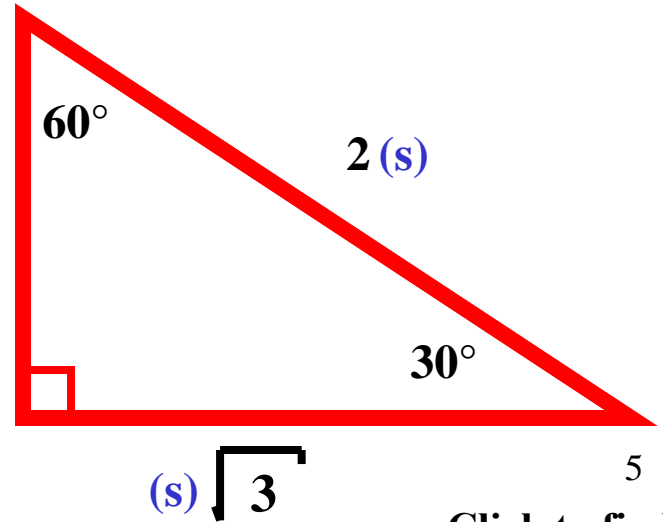
(2) $\sqrt{3}$

(.5) 1



(.5) $\sqrt{3}$

(s) 1



(s) $\sqrt{3}$

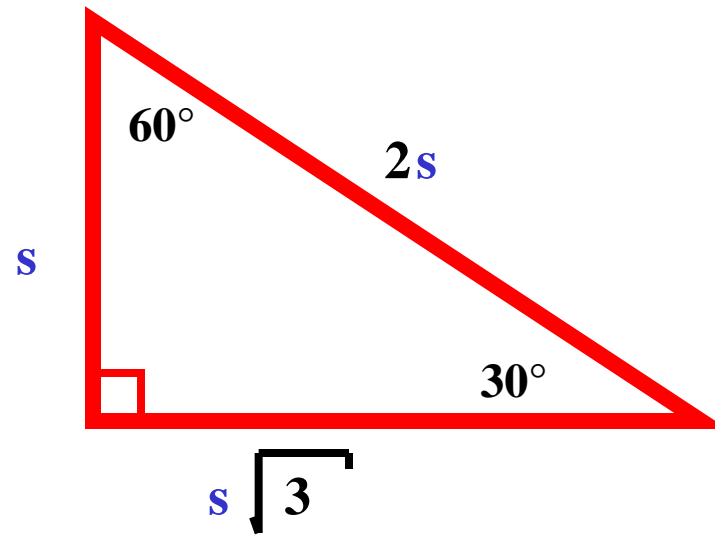
5

Click to find out...

7. Is this true for a triangle that is twice as big?

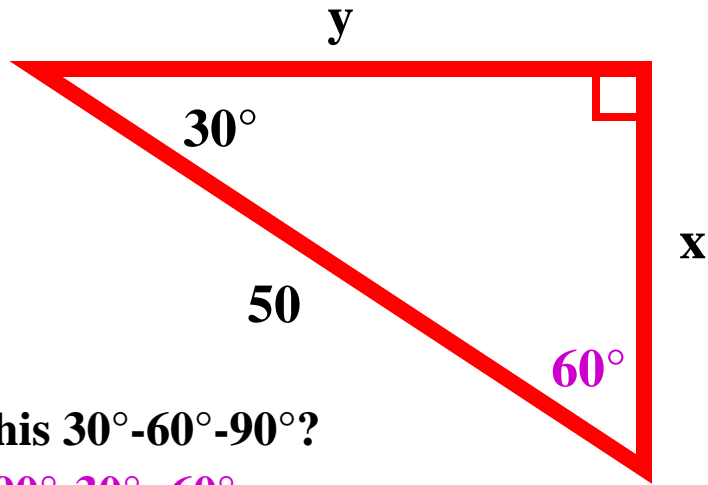
8. Is this true for a triangle that is half the original size?

9. What about a triangle that is "s" times bigger or Smaller?



In a 30° - 60° - 90° triangle, the hypotenuse is twice as long as the shorter leg, and the longer leg is $\sqrt{3}$ times as long as the shorter leg.

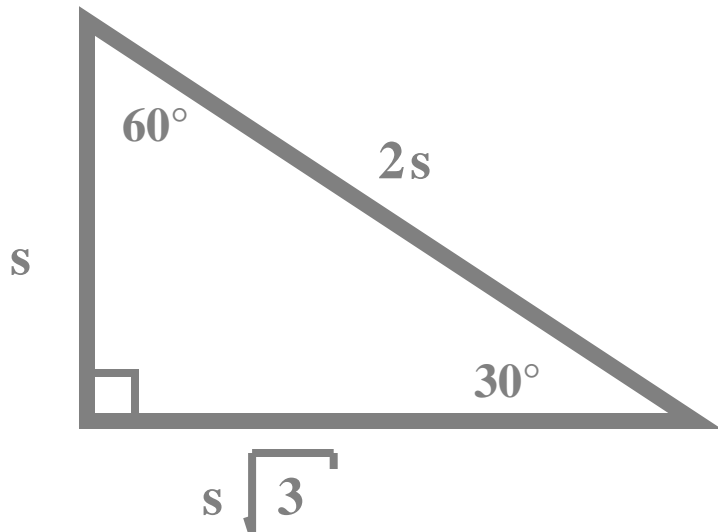
Find the values of the variables. Round your answers to the nearest hundredth.



Is this 30° - 60° - 90° ?

$$90^\circ - 30^\circ = 60^\circ$$

Then we know that:



$$2x = 50$$

$$\frac{2x}{2} = \frac{50}{2}$$

$$x = 25$$

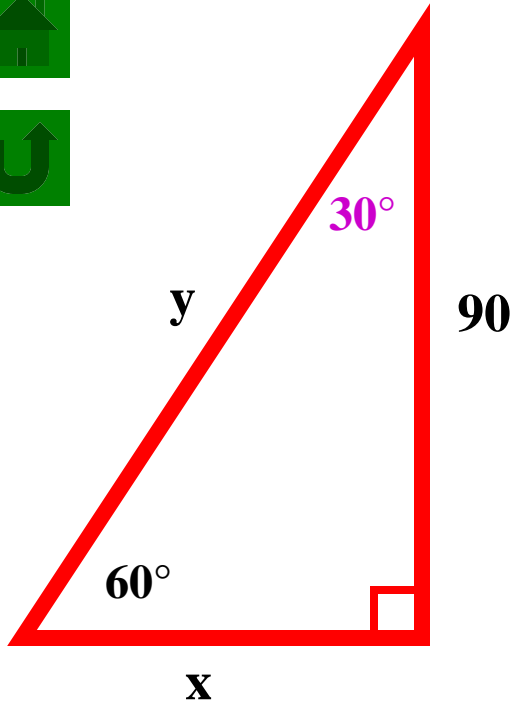
$$y = x\sqrt{3}$$

$$y = 25\sqrt{3}$$

OR

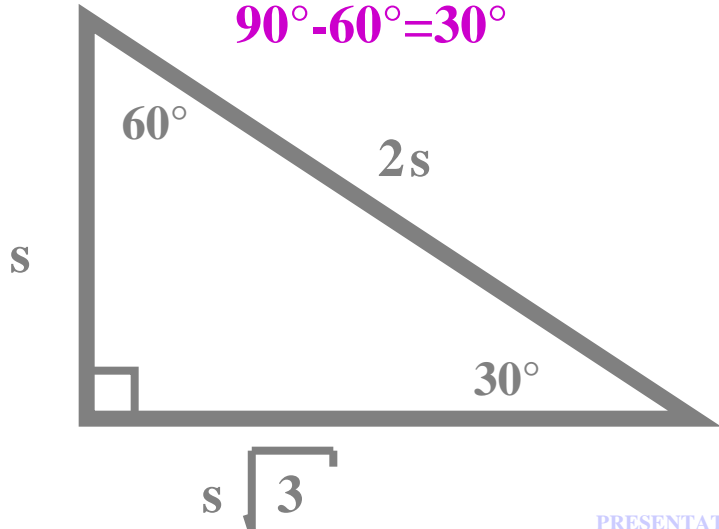
$$y \doteq 43.30$$

Find the values of the variables. Round your answers to the nearest unit. **Standard 20**



Is this a 30°-60°-90°?

$$90^\circ - 60^\circ = 30^\circ$$



$$90 = x \sqrt{3}$$

~~$$90 = x \sqrt{3}$$~~

$$\frac{90}{\sqrt{3}} = x$$

$$\frac{\sqrt{3}}{\sqrt{3}} \cdot \frac{90}{\sqrt{3}} = x$$

~~$$\frac{90\sqrt{3}}{(\sqrt{3})^2} = x$$~~

$$\frac{90\sqrt{3}}{3} = x$$

$$30\sqrt{3} = x$$

$$x = 30\sqrt{3}$$

$$2x = y$$

$$2(30\sqrt{3}) = y$$

$$60\sqrt{3} = y$$

$$y = 60\sqrt{3}$$

OR

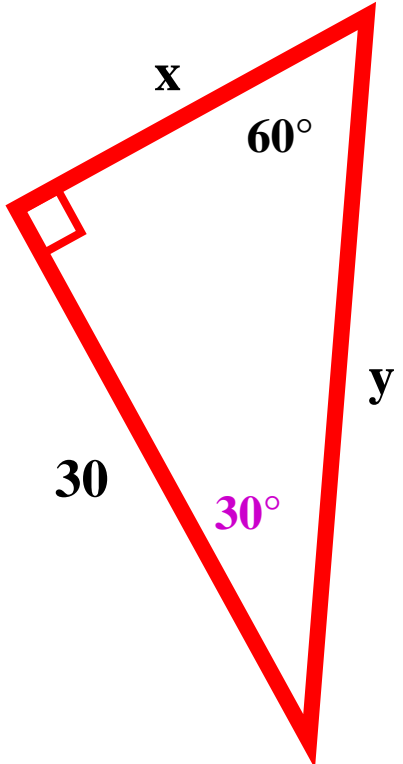
$$y \doteq 104$$

OR

$$x \doteq 52$$

Find the values of the variables. Find the exact answer.

Standard 20



$$30 = x \sqrt{3}$$

~~$$30 = x \sqrt{3}$$~~
~~$$\frac{30}{\sqrt{3}} = \frac{x \sqrt{3}}{\sqrt{3}}$$~~

$$\frac{\sqrt{3}}{\sqrt{3}} \cdot \frac{30}{\sqrt{3}} = x$$

~~$$\frac{30\sqrt{3}}{(\sqrt{3})^2} = x$$~~

$$\frac{30\sqrt{3}}{3} = x$$

$$10\sqrt{3} = x$$

$$x = 10\sqrt{3}$$

$$2x = y$$

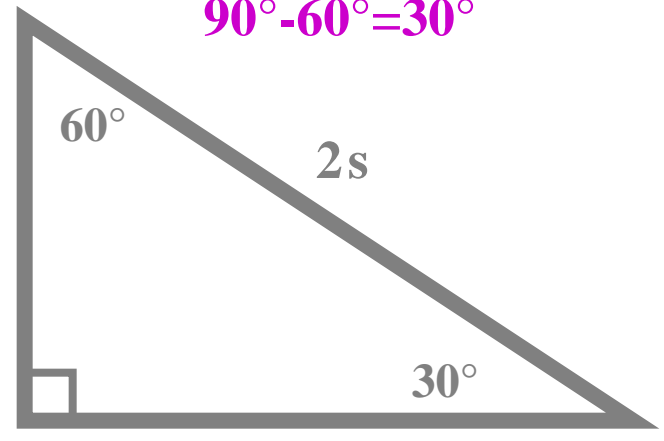
$$2(10\sqrt{3}) = y$$

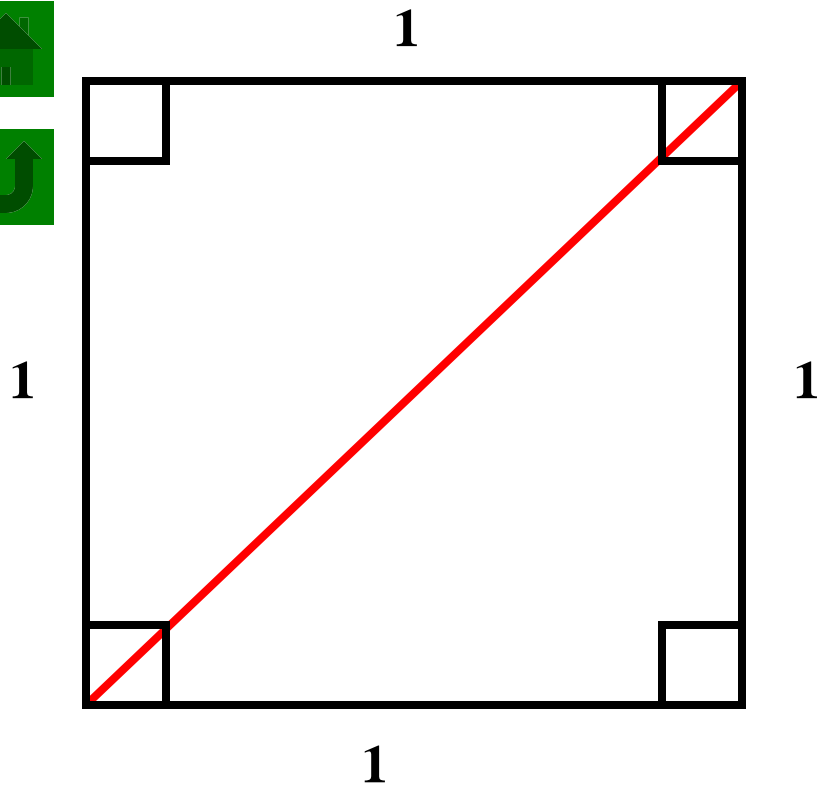
$$20\sqrt{3} = y$$

$$y = 20\sqrt{3}$$

Is this a 30°-60°-90°?

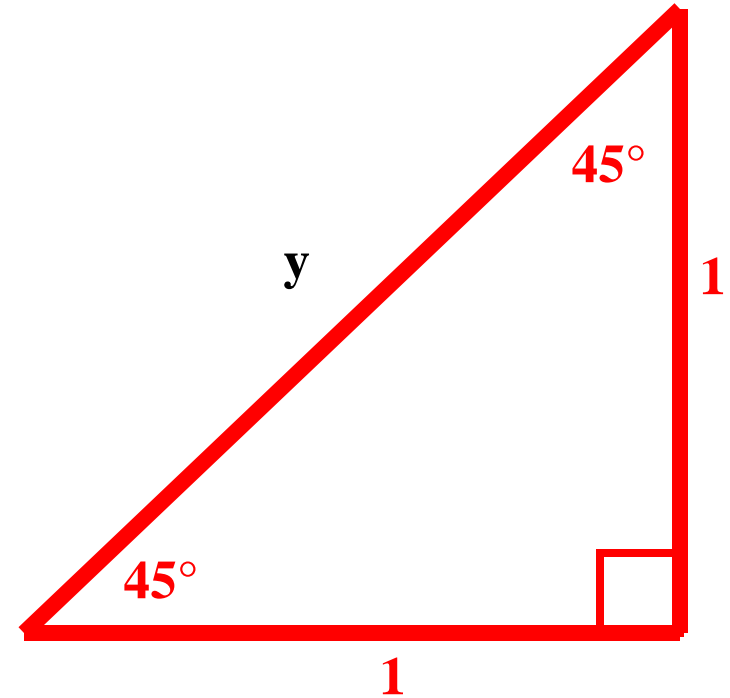
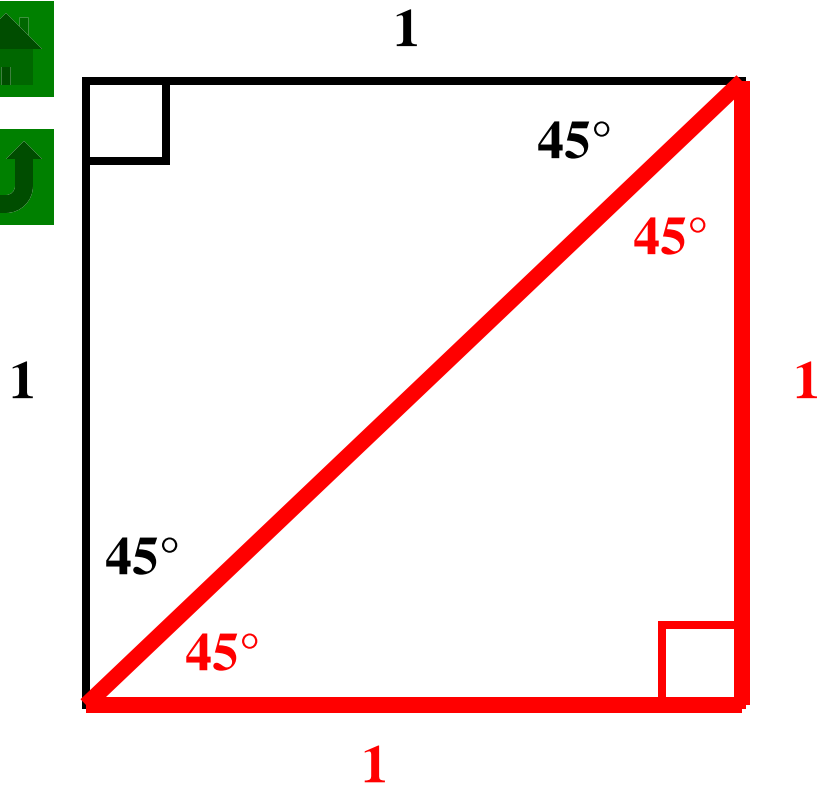
$$90^\circ - 60^\circ = 30^\circ$$





1. Let's draw a diagonal for the square above. The diagonal bisects the right angles of the square.

What kind of right triangles are form? Click to find out...



$$y^2 = 1^2 + 1^2$$

$$y^2 = 1 + 1$$

$$y^2 = 2$$

$$\sqrt{y^2} = \sqrt{2}$$

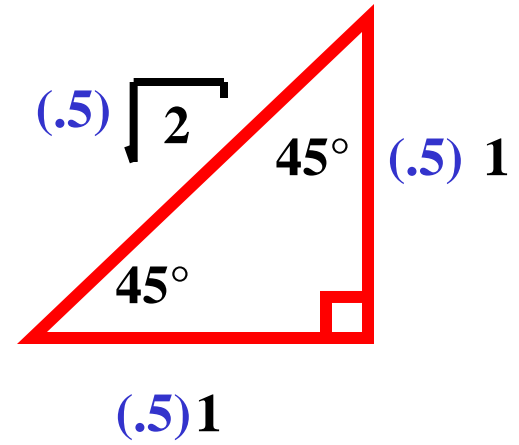
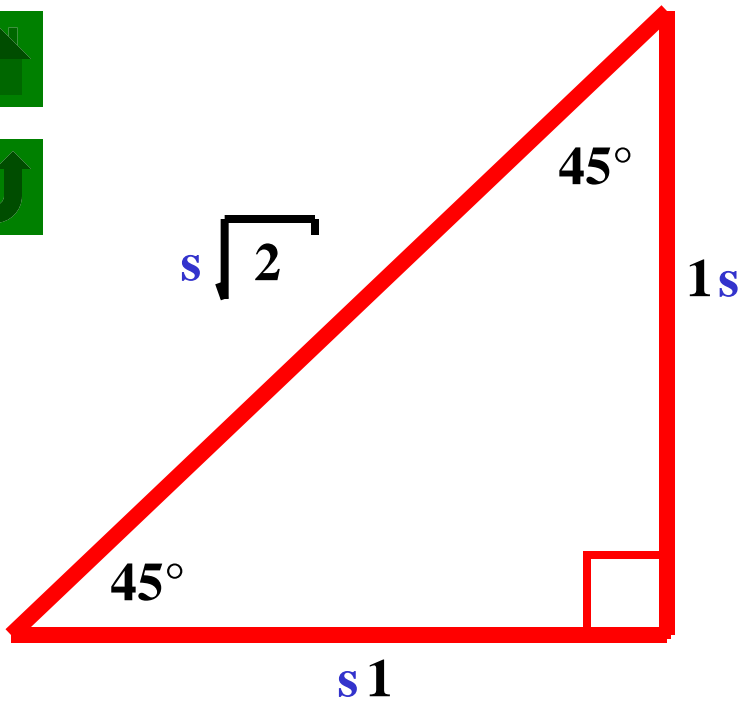
$$y = \sqrt{2}$$

2. The triangles are 45° - 45° - 90°

3. Let's draw the bottom triangle and label the hypotenuse as y

4. Let's apply the Pythagorean Theorem to find the hypotenuse.

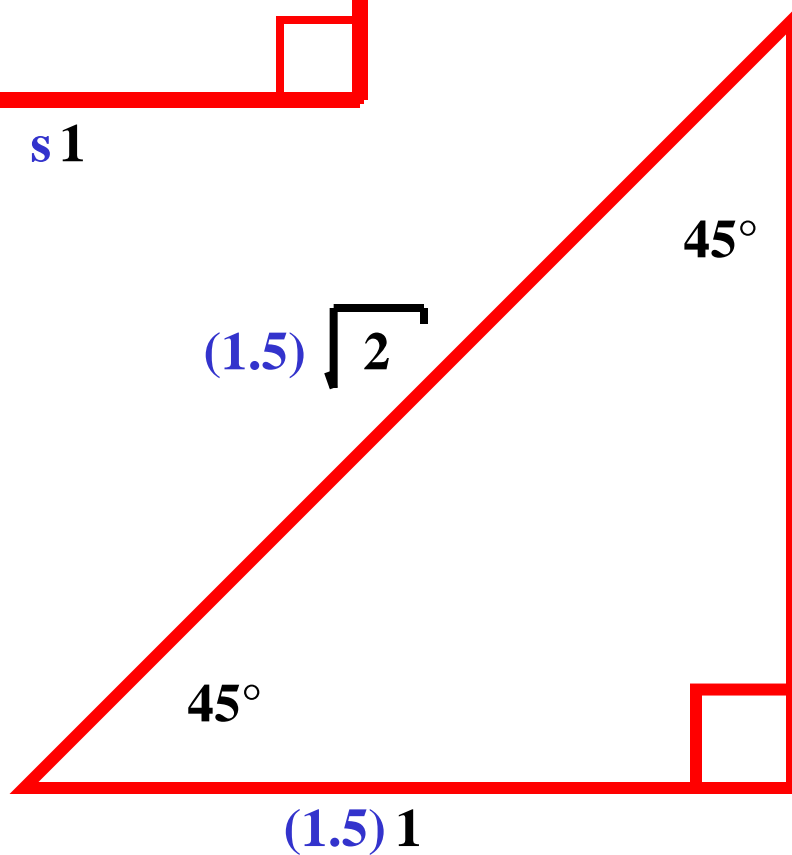
Can we generalize our findings? Click to find out...



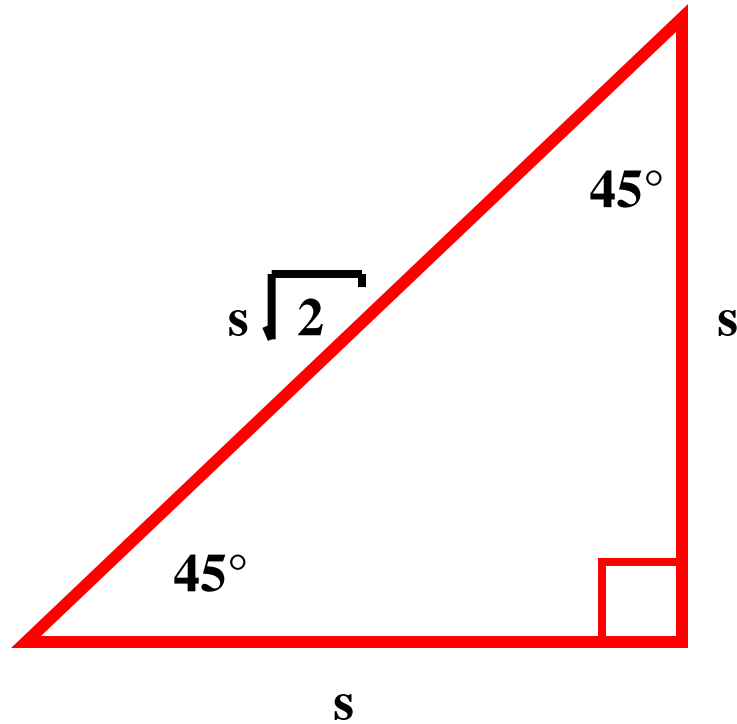
5. Let's draw a triangle half the size of the original.

6. Let's draw a triangle one and a half the size of the original.

(1.5) 1



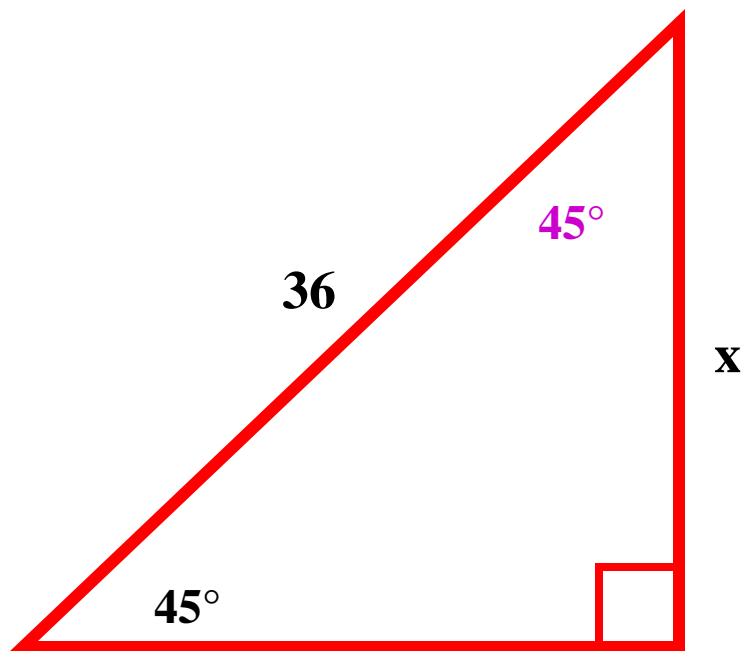
7. Let's draw a triangle S times the size of the original.



In a 45° - 45° - 90° triangle, the hypotenuse is $\sqrt{2}$ times as long as a leg.

Find the values of the variables. Round your answers to the nearest tenth.

Standard 20



$$36 = x\sqrt{2}$$

$$\frac{36}{\sqrt{2}} = \frac{x\sqrt{2}}{\sqrt{2}}$$

$$\frac{36\sqrt{2}}{\sqrt{2}\sqrt{2}} = x$$

If $y = x$

then $y = 18\sqrt{2}$

$$\frac{36\sqrt{2}}{(\sqrt{2})^2} = x$$

OR

$$y \doteq 25.5$$

$$\frac{36\sqrt{2}}{2} = x$$

$$18\sqrt{2} = x$$

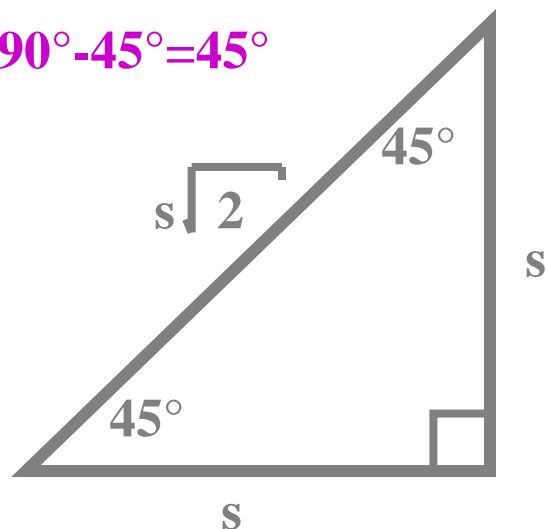
$$x = 18\sqrt{2}$$

OR

$$x \doteq 25.5$$

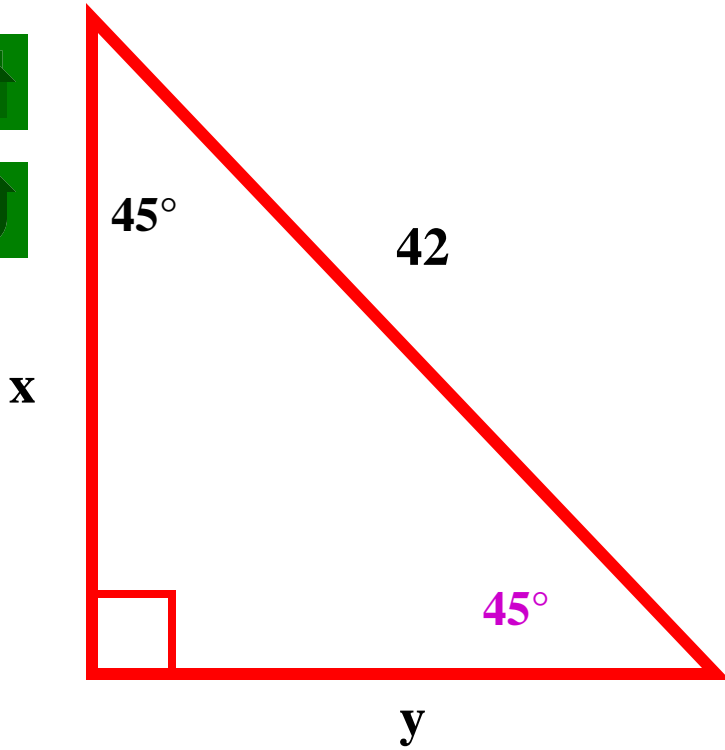
Is this a $45^\circ-45^\circ-90^\circ$?

$$90^\circ - 45^\circ = 45^\circ$$



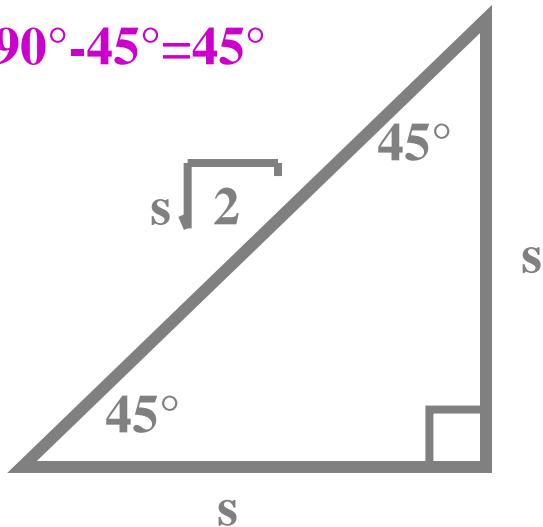
Find the values of the variables. Give an exact answer.

Standard 20



Is this a $45^\circ-45^\circ-90^\circ$?

$$90^\circ - 45^\circ = 45^\circ$$



$$42 = x\sqrt{2}$$

$$\frac{42}{\sqrt{2}} = \frac{x\sqrt{2}}{\sqrt{2}}$$

$$\frac{42\sqrt{2}}{\sqrt{2}} = x$$

$$\frac{42\sqrt{2}}{(\sqrt{2})^2} = x$$

$$\frac{42\sqrt{2}}{2} = x$$

$$21\sqrt{2} = x$$

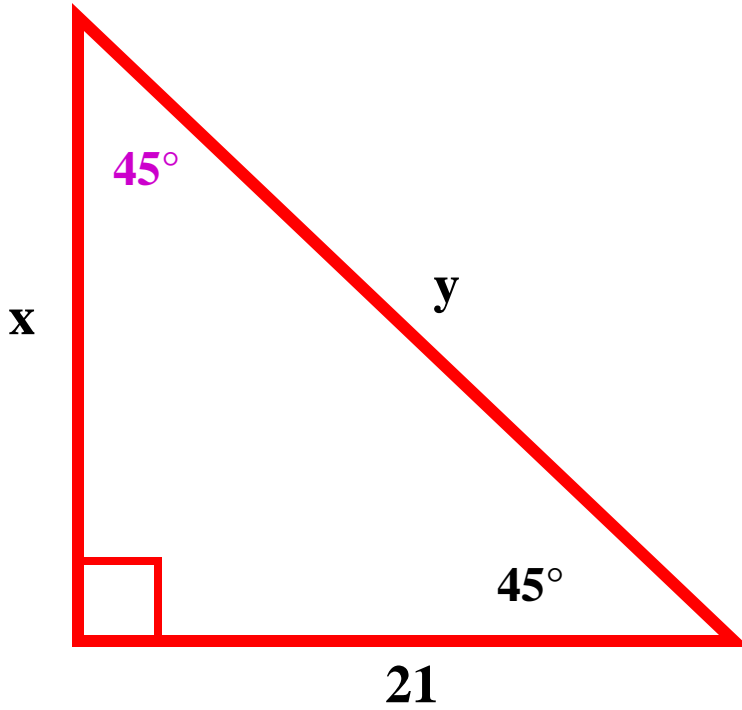
$$\boxed{x = 21\sqrt{2}}$$

If $y = x$

then

$$\boxed{y = 21\sqrt{2}}$$

Find the values of the variables. Give the exact answer.



$$x = 21$$

$$y = x \sqrt{2}$$

$$y = 21\sqrt{2}$$

Is this a 45°-45°-90°?

$$90^\circ - 45^\circ = 45^\circ$$

